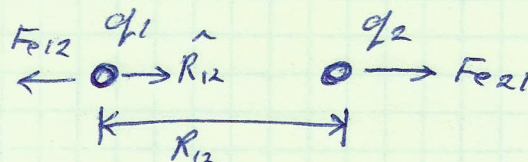


- Class information sheet
- Syllabus - handout
- Motivation to study electromagnetics:
 - foundation for optics, circuits, RF, communication, etc
 - understanding from one field can be applied to many others
 - eg. reflections, impedance, wave behavior, etc.
 - one of the four fundamental forces:
 - nuclear (strong), EM, weak, gravity

• Electric fields

- Surrounds charged particles
- causes forces on other charged particles



$$\vec{F}_{21} = \hat{R}_{12} \frac{q_1 q_2}{4\pi \epsilon_0 R_{12}^2} \quad \text{Coulomb's Law}$$

notation: bold $\rightarrow$ vector, sometimes use $\vec{X}$ (arrow)
 $\hat{x}$ "hat" $\rightarrow$ unit vector
 $X_{ab} \rightarrow$ "from a to b " or "caused on a by b "

Electric field intensity

$$\vec{E} = \hat{R} \frac{q}{4\pi \epsilon_0 R^2}$$

force on another charge q'

$$\vec{F}_e = q' \vec{E}$$

constants

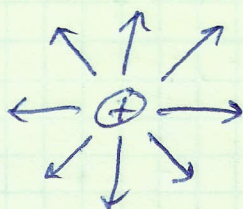
$$e = 1.6 \times 10^{-19} \text{ C}$$

electron charge

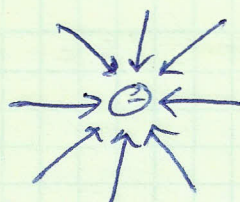
$$\epsilon_0 = 8.854 \times 10^{-12} \text{ F/m}$$

electric permittivity of free space

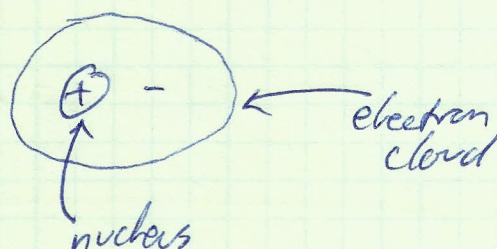
- Conservation of electric charge
 - charge (net, total) cannot be created or destroyed
- Principle of linear superposition
 - total vector electric field is due to the vector sum of electric fields from all sources
- Field lines



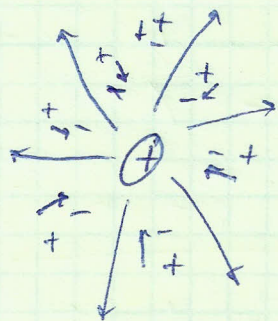
Electric dipole



polarized atom



Electric field screening by dielectric material



$$E = \hat{R} \frac{q}{4\pi\epsilon R^2}$$

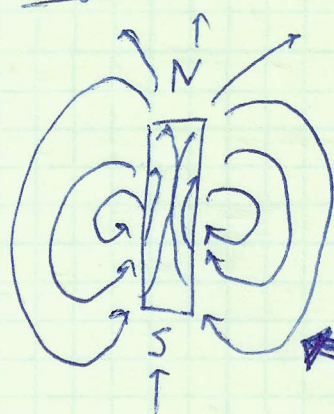
$$\epsilon = \epsilon_r \epsilon_0$$

↑ relative permittivity

- Electric flux density

$$\vec{D} = \epsilon \vec{E}$$

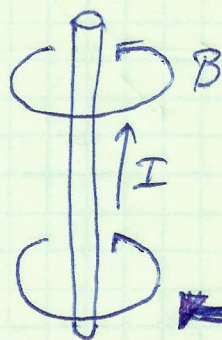
Magnetic Fields



• No magnetic monopoles

• Caused by currents - macroscopic or microscopic (spins)

Bar Magnet



$$B = \oint \frac{\mu_0 I}{2\pi R}$$

$\mu_0 = 4\pi \times 10^{-7} \text{ H/m}$
permeability of
free space

Current in wire

Right hand rule



$$\mu = \mu_r \mu_0$$

relative permeability

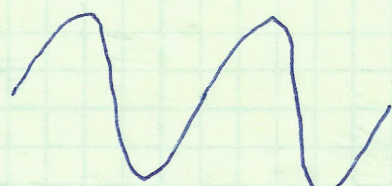
$$\vec{B} = \mu \vec{H}$$

H = magnetic field intensity

• Waves

- Can transfer energy and information
- travel with velocity (3×10^8 m/s for light in free space)
- often can apply linearity
 - when one wave doesn't affect others
 - treat each independently, add results
- types: plane, cylindrical, spherical, surface
- general form

$$y(x, t) = A \cos \left(\underbrace{\frac{2\pi t}{T}}_{\text{period}} - \underbrace{\frac{2\pi x}{\lambda}}_{\text{wavelength}} - \phi_0 \right)$$



T in time
or λ in space

set $y = \text{constant}$
find $\frac{dx}{dt}$

- waves move with phase velocity $\frac{dx}{dt} = \frac{\lambda}{T} = v_p$
- waves have a frequency $f = \frac{1}{T}$ (in Hz)

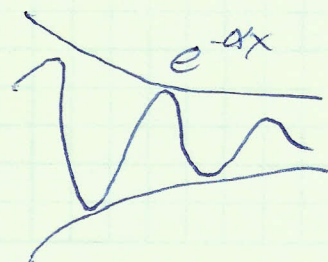
$$v_p = f\lambda = c = 3 \times 10^8 \text{ m/s for EM waves in free space}$$

angular velocity $\omega = 2\pi f$

wavenumber $\beta = \frac{2\pi}{\lambda}$

- Lossy medium

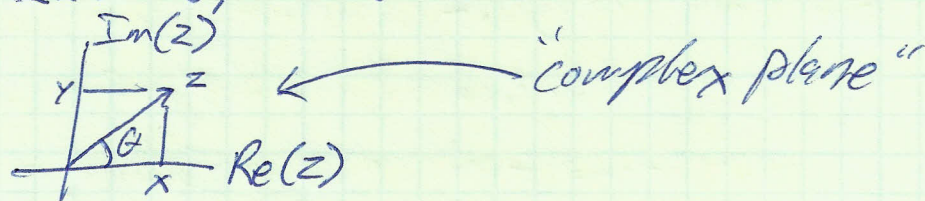
$$y(x, t) = A e^{-\alpha x} \cos(\omega t - \beta x + \phi_0)$$



Complex Numbers

$$z = x + jy$$

$$j = \sqrt{-1}$$



$$z = |z|e^{j\theta} = |z|(\cos\theta + j\sin\theta)$$

$$|z| = \sqrt{x^2 + y^2}$$

$$\theta = \tan^{-1}(y/x)$$

$$\text{complex conjugate } z^* = x - jy = |z|e^{-j\theta}$$

$$|z| = \sqrt{zz^*}$$

Phasors

$$\text{time domain } V(t) = V_0 \cos(\omega t + \phi)$$

$$\text{phasor representation } V(t) = \text{Re}[V_0 e^{j(\omega t + \phi)}]$$

$$\downarrow$$

$$\tilde{V} e^{j\omega t}$$

$$\text{extract mag/phase} \rightarrow \tilde{V} = V_0 e^{j\phi}$$

separate from time variation

Makes differentiation or integration easier

$$\frac{d}{dt}(\tilde{V} e^{j\omega t}) = j\omega \tilde{V} e^{j\omega t}$$

don't need to keep track of arbitrary sines, cosines